

Formalizing Robustness in Neural Networks: Explainability, Uncertainty, and Intervenability



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Tutorial Materials

Accessible Online



<https://alregib.ece.gatech.edu/aaai-2024-tutorial/>
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AAAI 2024 Tutorial



Presented by: *Ghassan AlRegib, and Mohit Prabhushankar*
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Duration: Half Day (3 hours, 30 mins)

Title: Formalizing Robustness in Neural Networks: Explainability, Uncertainty, and Intervenability



Expectation vs Reality of Deep Learning



Deep Learning

Expectation vs Reality

LATEST TRICKS

Rotating objects in an image confuses DNNs, probably because they are too different from the types of image used to train the network.

Stop



Dumb-bell

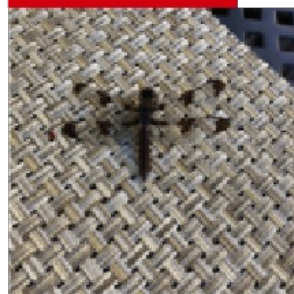


Racket

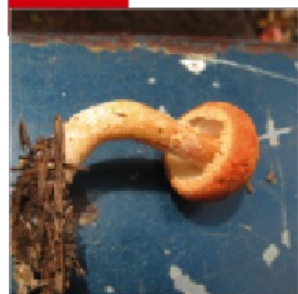


Even natural images can fool a DNN, because it might focus on the picture's colour, texture or background rather than picking out the salient features a human would recognize.

Manhole cover



Pretzel



©nature



Deep Learning

Expectation vs Reality

*“The best-laid plans of sensors and networks
often go awry”*

- Engineers, probably



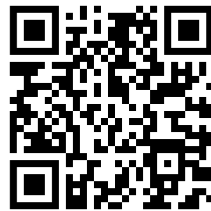
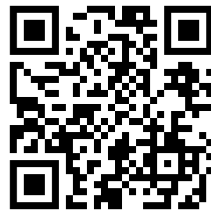
Deep Learning

Requirements and Challenges

Requirements: Deep Learning-enabled systems must predict correctly on novel data

Novel data sources:

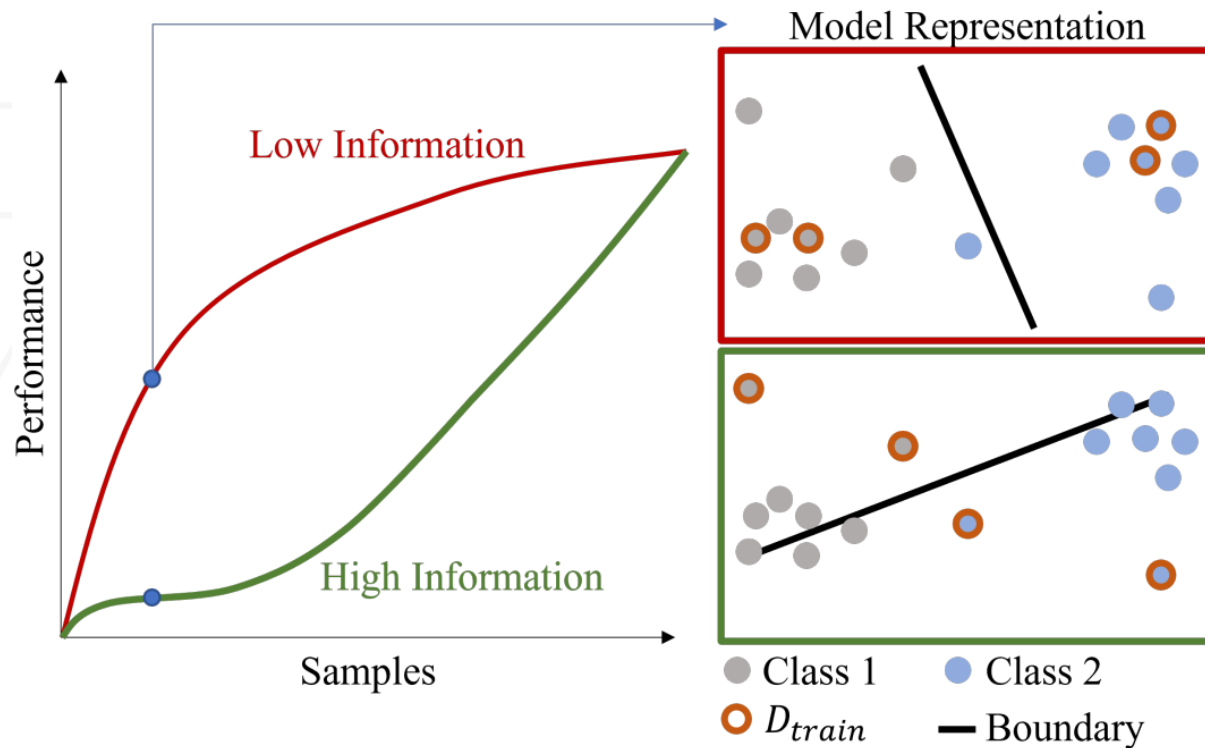
- Test distributions
- Anomalous data
- Out-Of-Distribution data
- Adversarial data
- Corrupted data
- Noisy data
- New classes
- ...



Deep Learning at Training

Overcoming Challenges at Training: Part 1

The most novel/aberrant samples should not be used in early training



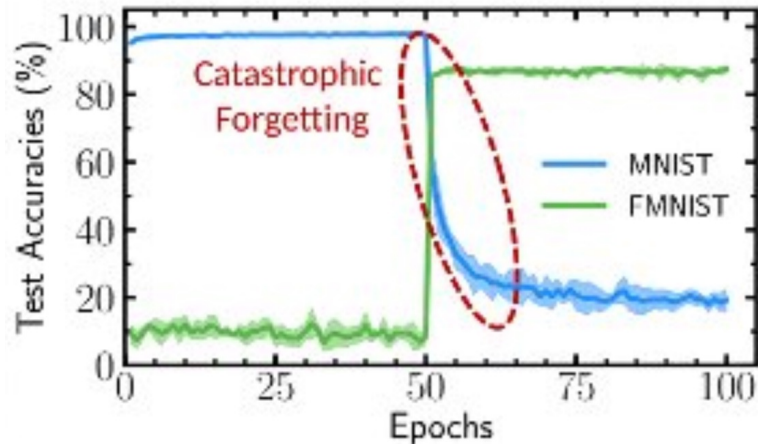
- The first instance of training must occur with less informative samples
- Ex: For autonomous vehicles, less informative means
 - Highway scenarios
 - Parking
 - No accidents
 - No aberrant events

Novel samples = Most Informative

Deep Learning at Training

Overcoming Challenges at Training: Part 2

Subsequent training must not focus only on novel data



- The model performs well on the new scenarios, while forgetting the old scenarios
- A number of techniques exist to overcome this trend
- However, they affect the overall performance in large-scale settings
- It is not always clear **if and when** to incorporate novel scenarios in training

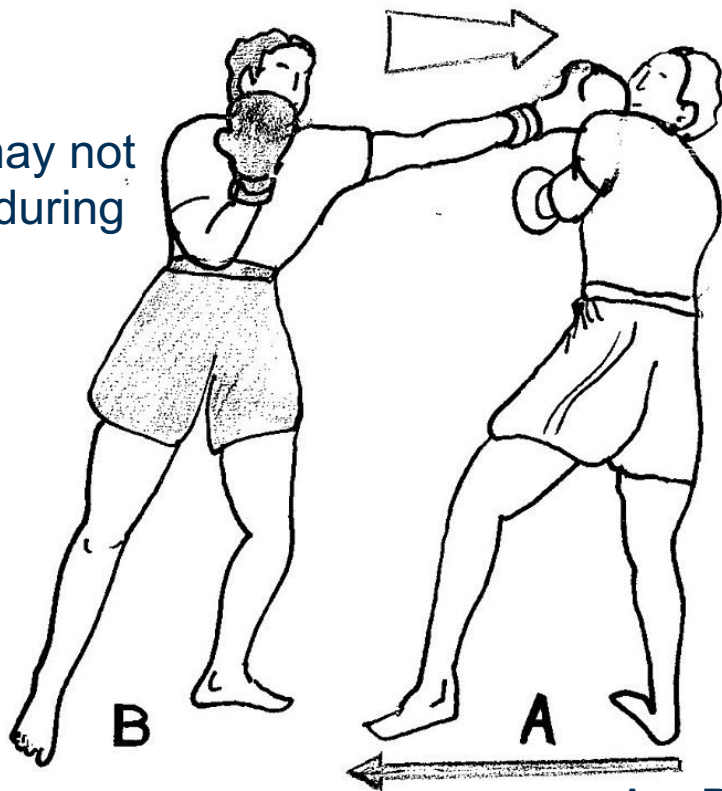


Deep Learning at Training

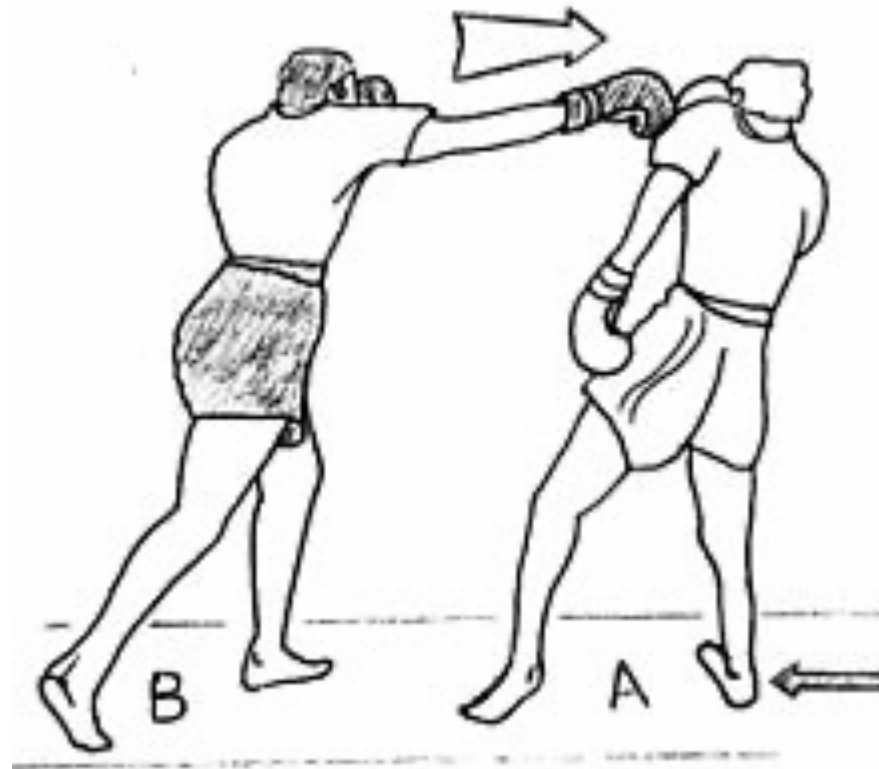
Overcoming Challenges at Training

Novel data packs a 1-2 punch!

Novel data may not be available during training



A = Deep Neural Networks
B = Novel data



Even if available, novel data does not easily fit into either the earlier or later stages of training

Deep Learning at Inference

Overcoming Challenges at Inference

We must handle novel data at Inference!!

Novel data sources:

- Test distributions
- Anomalous data
- Out-Of-Distribution data
- Adversarial data
- Corrupted data
- Noisy data
- New classes
- ...

Model Train



At Inference



Objective

Objective of the Tutorial

To discuss methodologies that promote robustness in neural networks at inference

- Part 1: Inference in Neural Networks
- Part 2: Explainability at Inference
- Part 3: Uncertainty at Inference
- Part 4: Intervenability at Inference
- Part 5: Conclusions and Future Directions



Robust Neural Networks

Part I: Inference in Neural Networks



Objective

Objective of the Tutorial

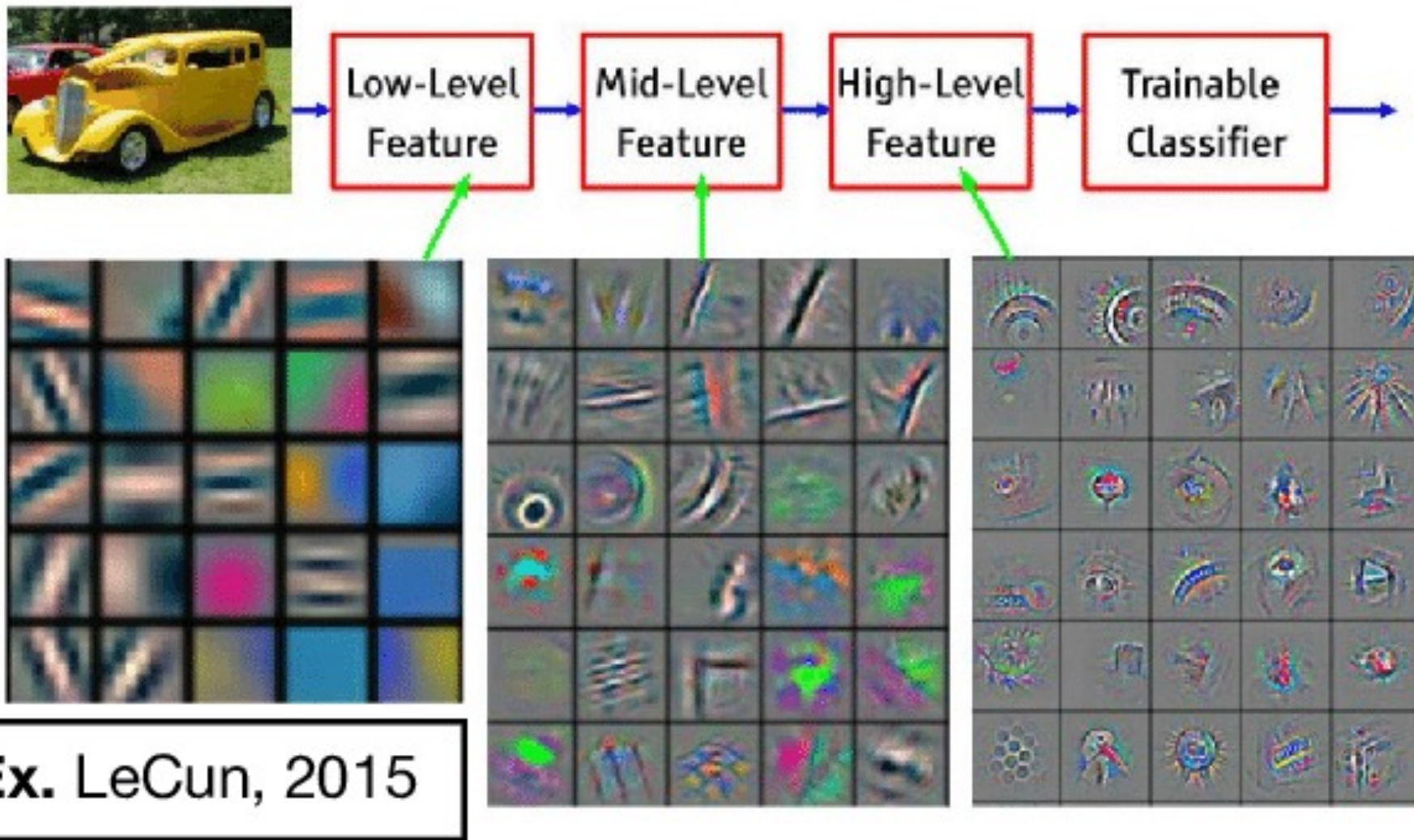
To discuss methodologies that promote robustness in neural networks at inference

- **Part 1: Inference in Neural Networks**
 - Neural Network Basics
 - Robustness in Deep Learning
 - Information at Inference
 - Challenges at Inference
 - Gradients at Inference
- Part 2: Explainability at Inference
- Part 3: Uncertainty at Inference
- Part 4: Intervenability at Inference
- Part 5: Conclusions and Future Directions



Deep Learning

Overview



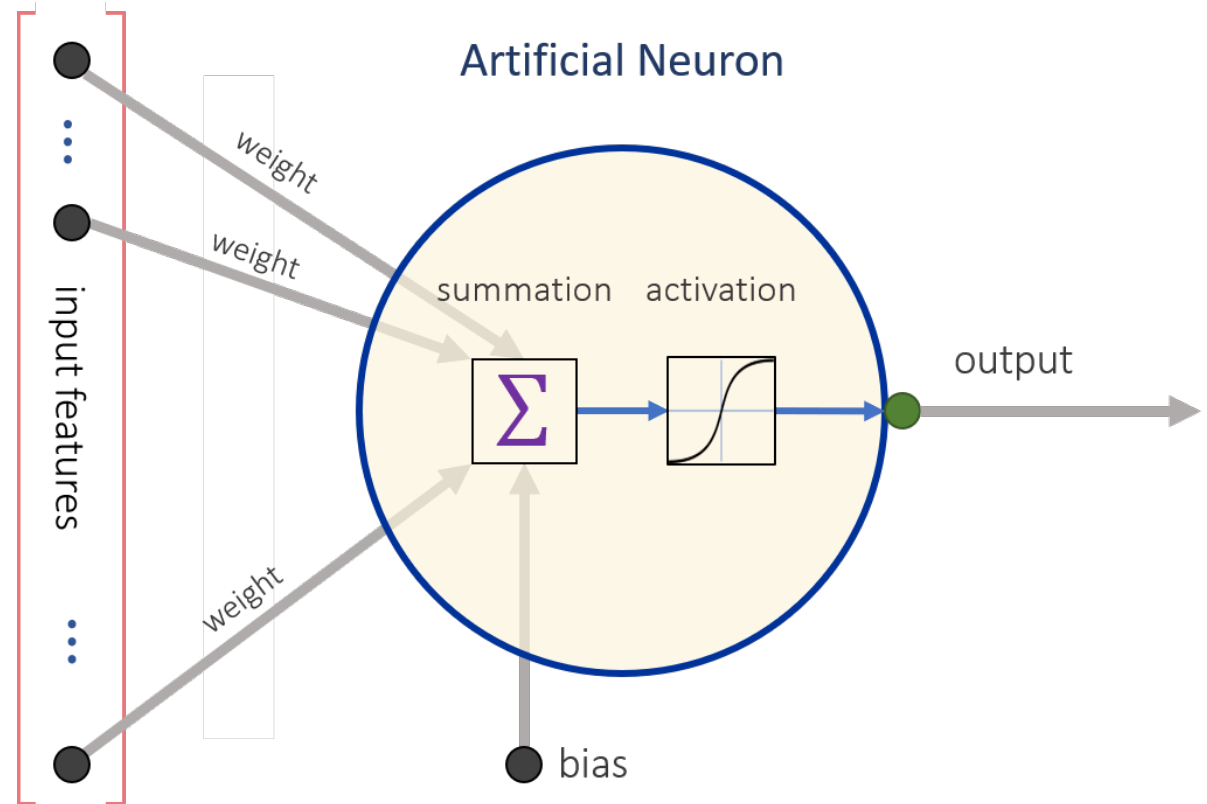
Deep Learning

Neurons

The underlying computation unit is the Neuron

Artificial neurons consist of:

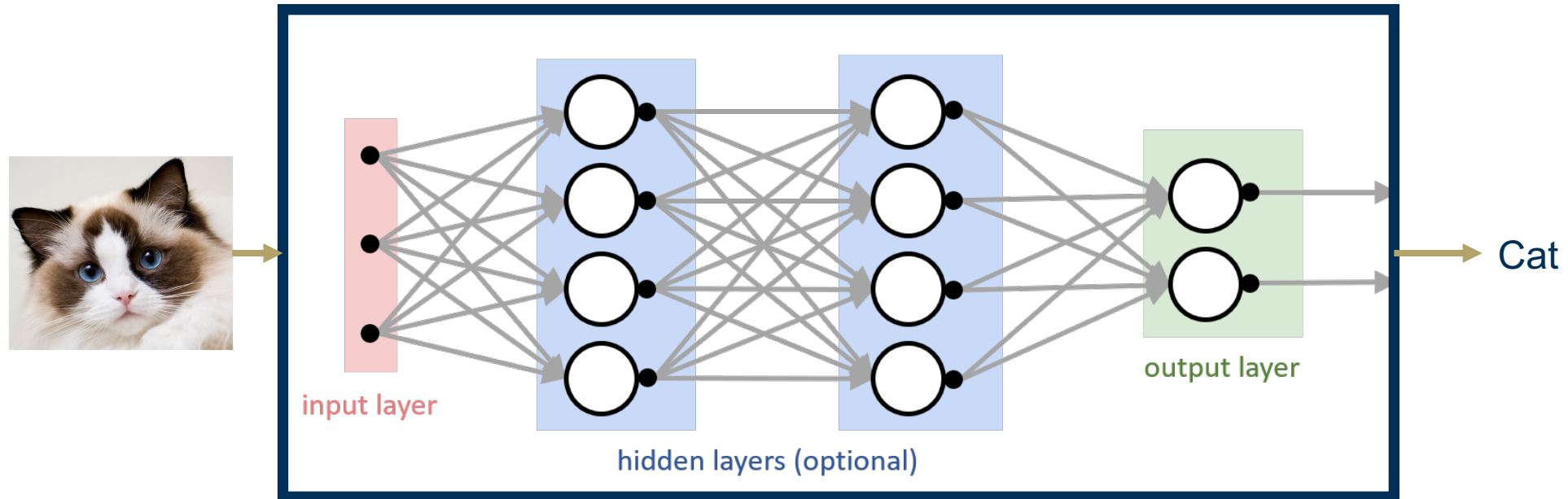
- A single output
- Multiple inputs
- Input weights
- A bias input
- An activation function



Deep Learning

Artificial Neural Networks

Neurons are stacked and densely connected to construct ANNs



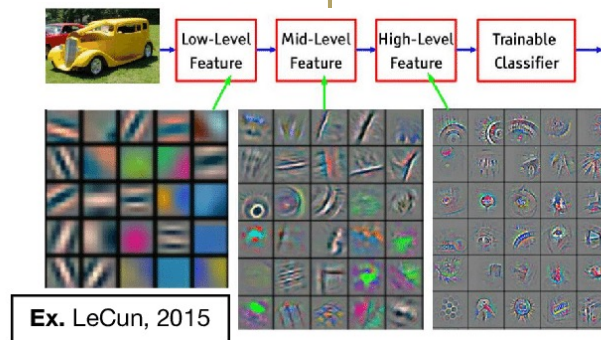
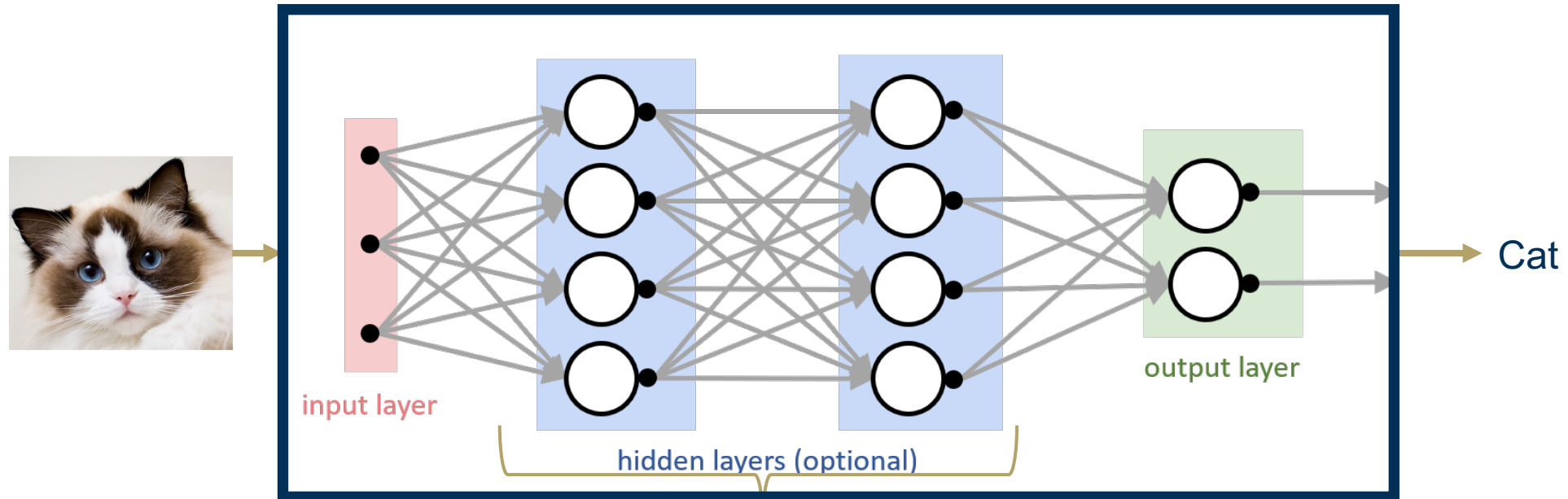
Typically, a neuron is part of a network organized in layers:

- An input layer (Layer 0)
- An output layer (Layer K)
- Zero or more hidden (middle) layers (Layers $1 \dots K - 1$)

Deep Learning

Convolutional Neural Networks

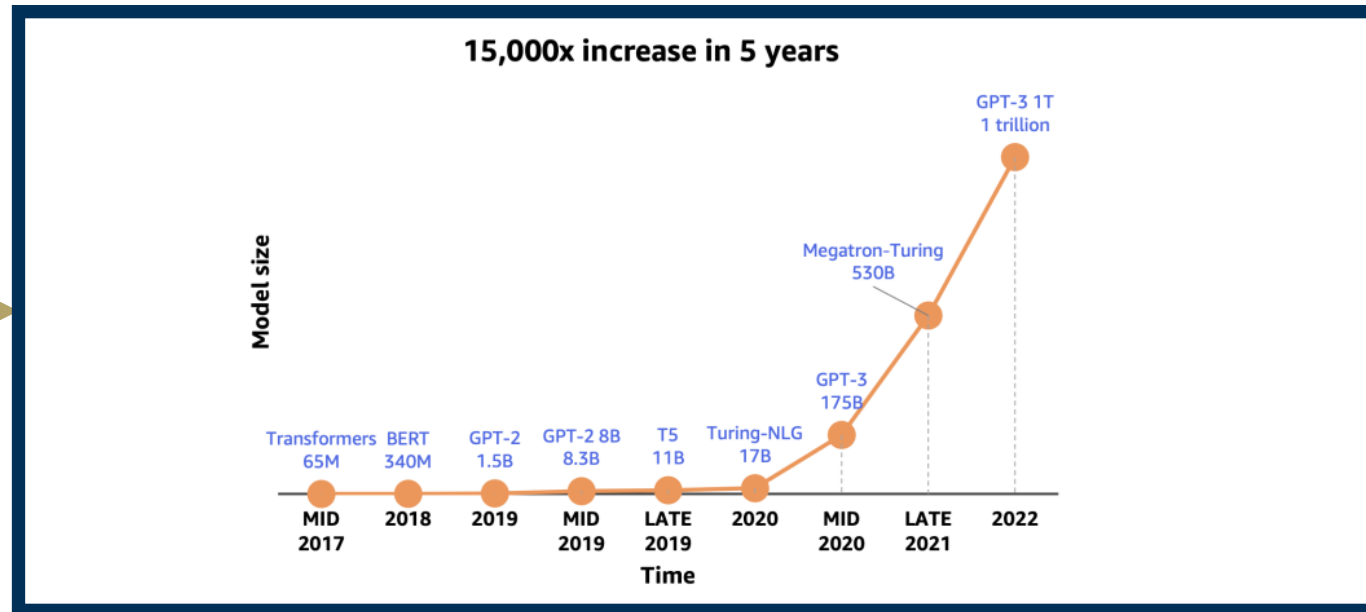
Stationary property of images allow for a small number of convolution kernels



Deep Deep Deep Deep Deep ... Learning

Recent Advancements

Transformers, Large Language Models and Foundation Models



Cat

Primary reasons for advancements:

1. Expanded interests from the research community
2. Computational resources availability
3. **Big data availability**

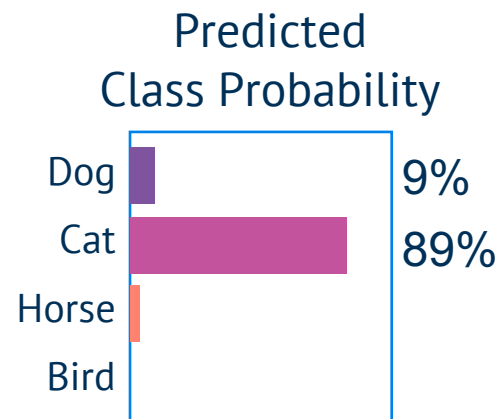
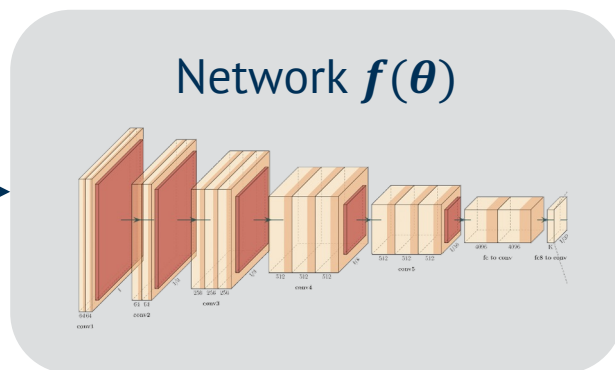
Deep Learning at Inference

Classification

Given : One network, One image. Required: Class Prediction



x



If $x \in \chi$, the data is **not novel**

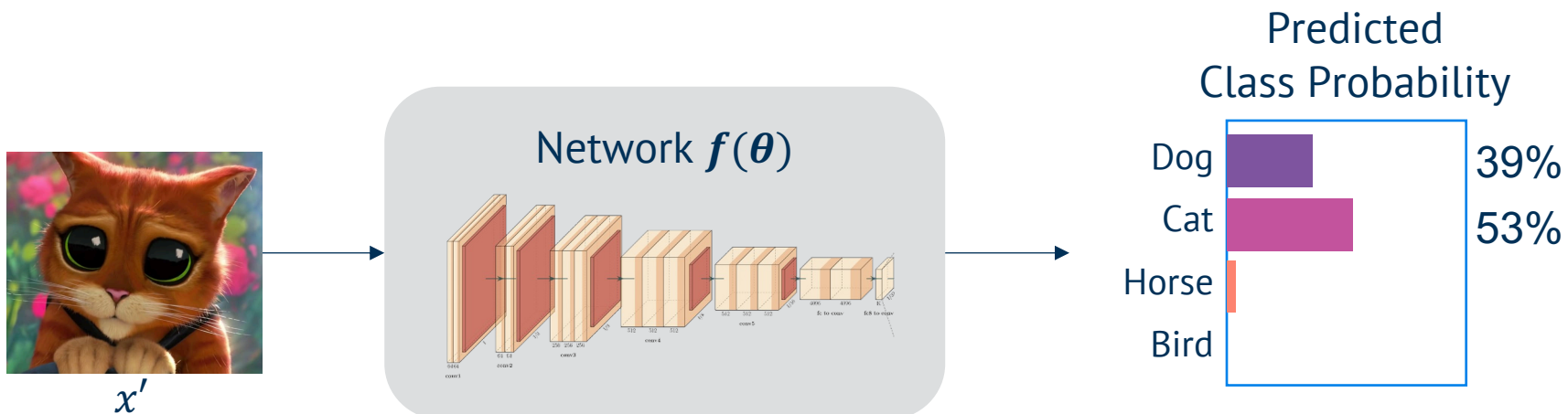
$$\hat{y} = f(x)$$
$$y = \operatorname{argmax}_i \hat{y}$$
$$p(\hat{y}) = T(f(x))$$

\hat{y} = Logits
 y = Predicted Class
 $p(\hat{y})$ = Probabilities
 $f(\cdot)$ = Trained Network
 χ = Training data

Deep Learning at Inference

Robust Classification in Deep Networks

Deep learning robustness: Correctly predict class even when data is novel



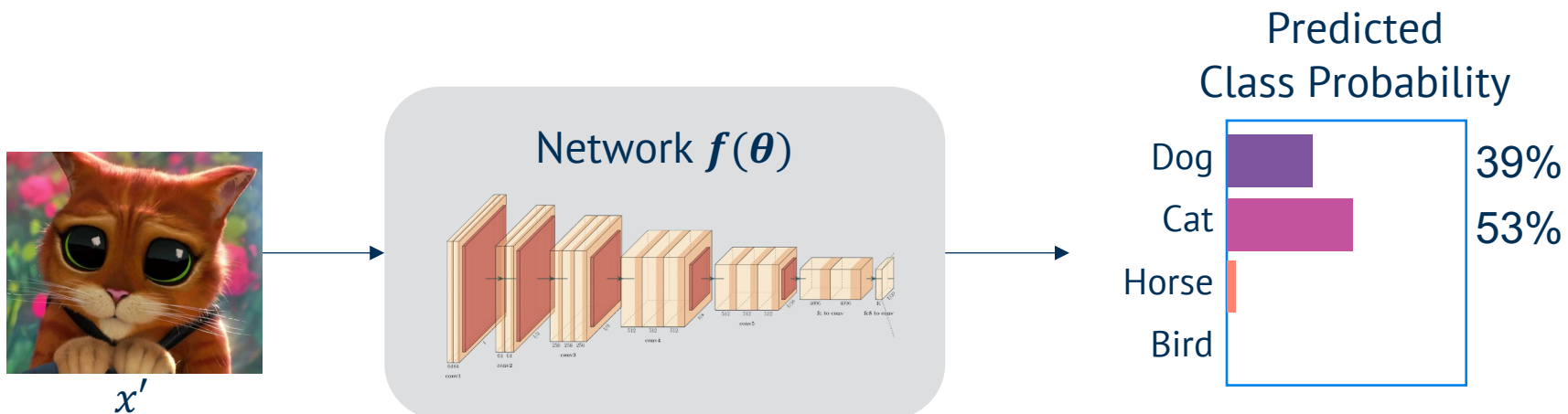
If $x \in \chi$, the data is **novel**

$$\begin{aligned} \hat{y} &= f(x' + \epsilon) & \hat{y} &= \text{Logits} \\ y &= \operatorname{argmax}_i \hat{y} & y &= \text{Predicted Class} \\ p(\hat{y}) &= T(f(x' + \epsilon)) & p(\hat{y}) &= \text{Probabilities} \\ & & f(\cdot) &= \text{Trained Network} \\ & & \chi &= \text{Training data} \\ & & \epsilon &= \text{Noise} \end{aligned}$$

Deep Learning at Inference

Robust Classification in Deep Networks

Deep learning robustness: Correctly predict class even when data is novel



To achieve robustness at Inference, we need the following:

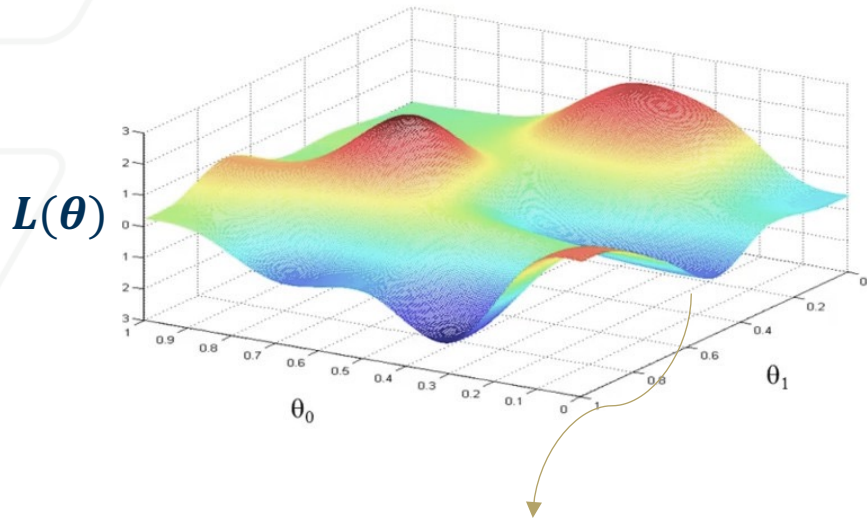
- **Information** provided by the novel data as a **function of training distribution**
- Methodology to **extract information** from novel data
- **Techniques** that utilize the information from novel data

Why is this Challenging?

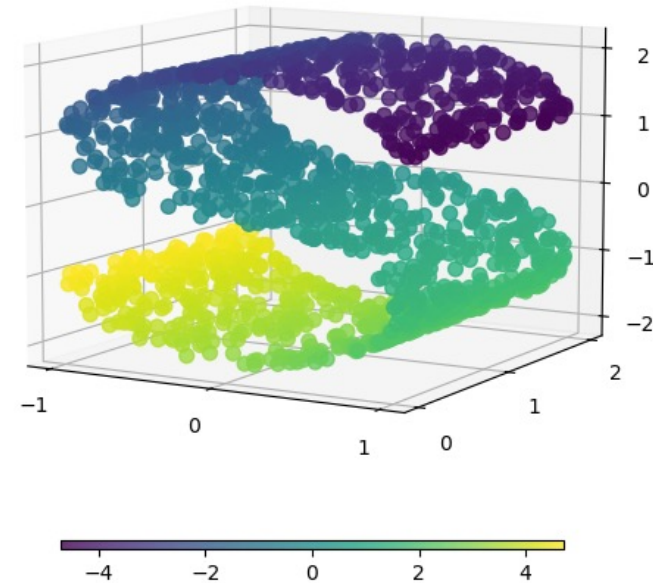
Challenges at Inference

A Quick note on Manifolds..

Manifolds are compact topological spaces that allow exact mathematical functions



Toy visualizations generated using functions
(and thousands of generated data points)

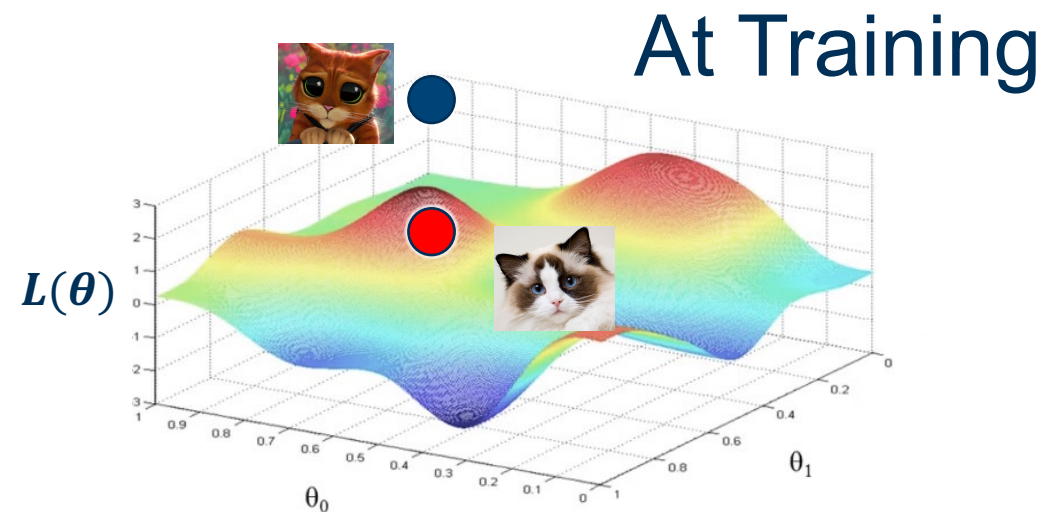
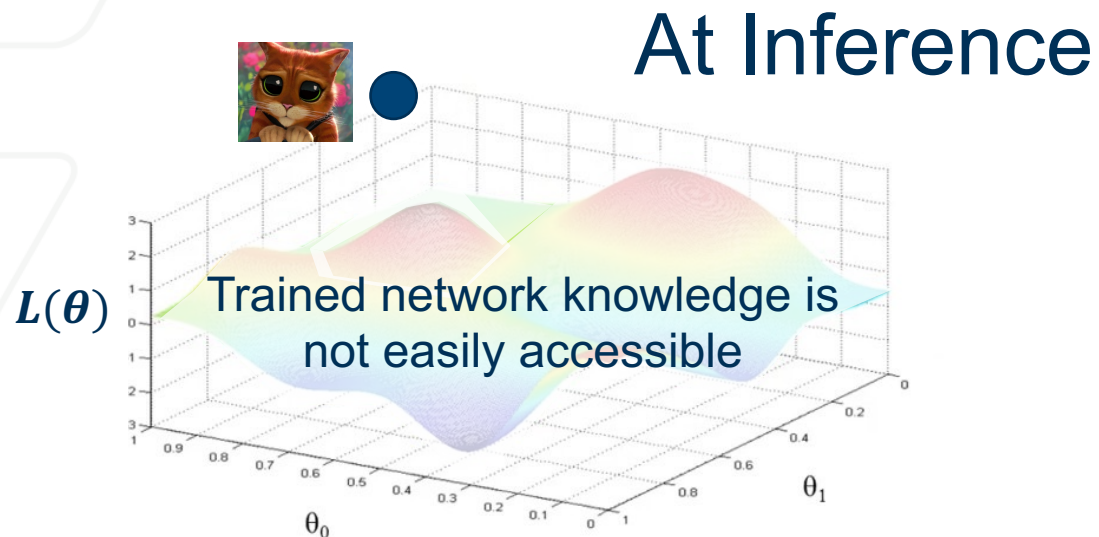


Real data visualizations generated using
dimensionality reduction algorithms (Isomap)

Challenges at Inference

Inference

However, at inference only the test data point is available and the underlying structure of the manifold is unknown

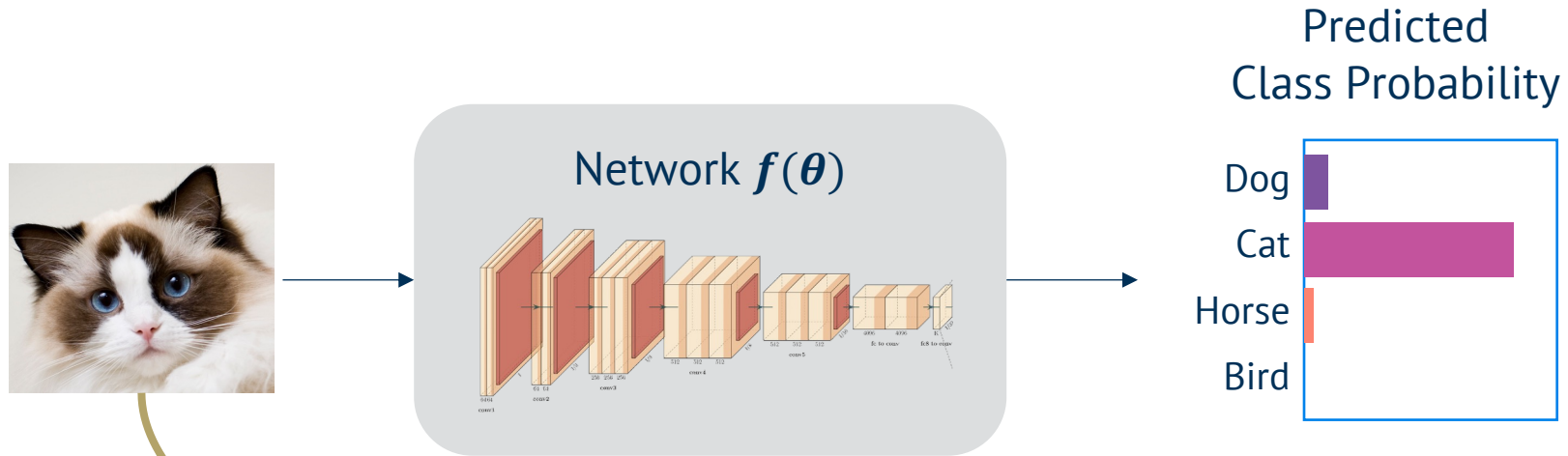


At training, we have access to all training data.

Information at Inference

Fisher Information

Colloquially, Fisher Information is the “surprise” in a system that observes an event

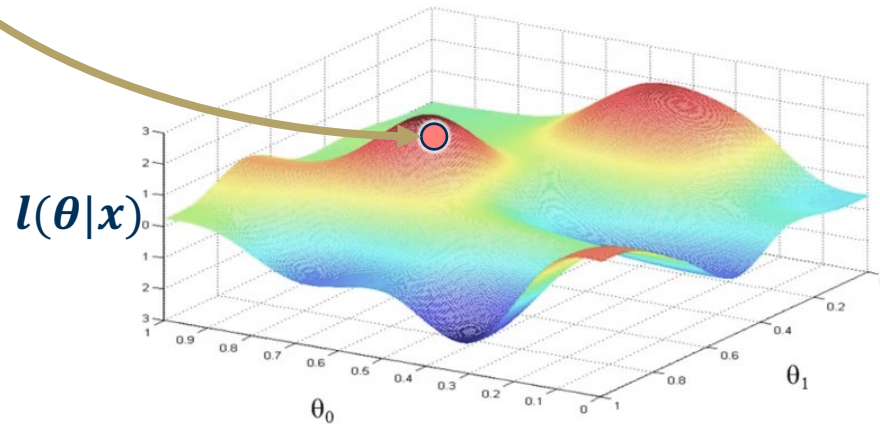


Fisher Information

$$I(\theta) = \text{Var}\left(\frac{\partial}{\partial \theta} l(\theta|x)\right)$$

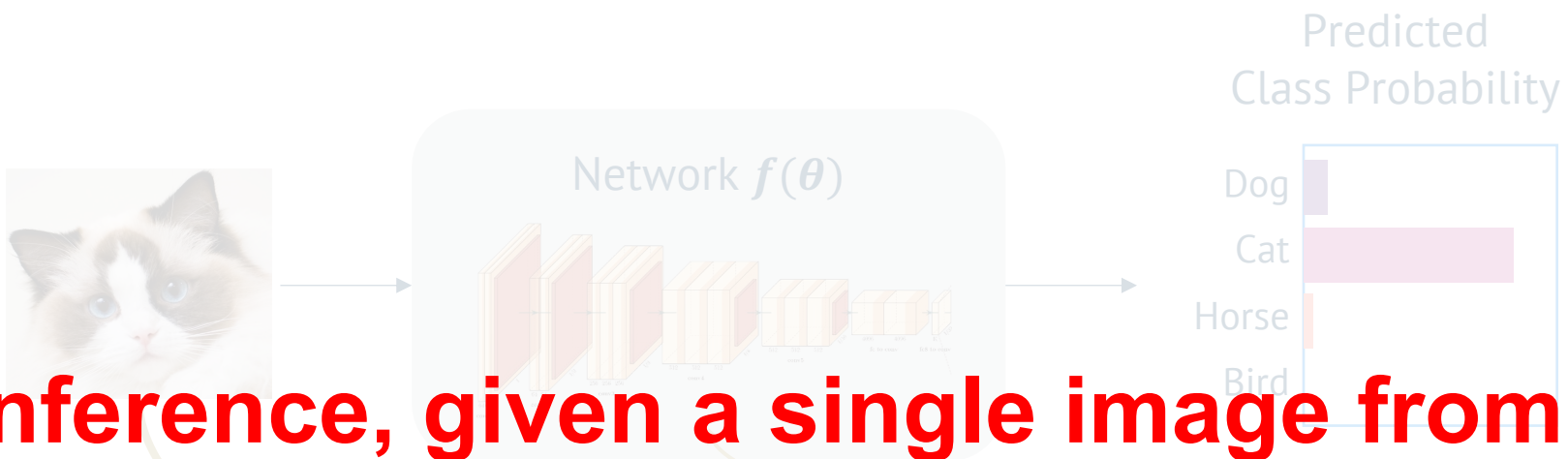
θ = Statistic of distribution
 $l(\theta | x)$ = Likelihood function

Likelihood function

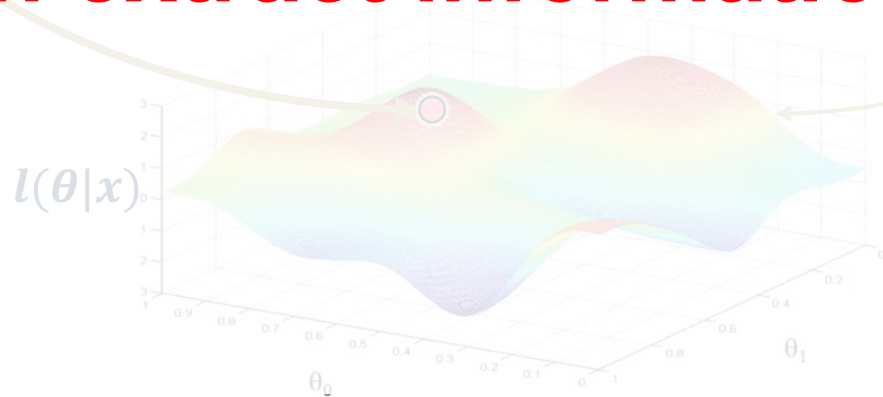


Information at Inference

Information at Inference



At inference, given a single image from a single class, we can extract information about other classes



Likelihood function

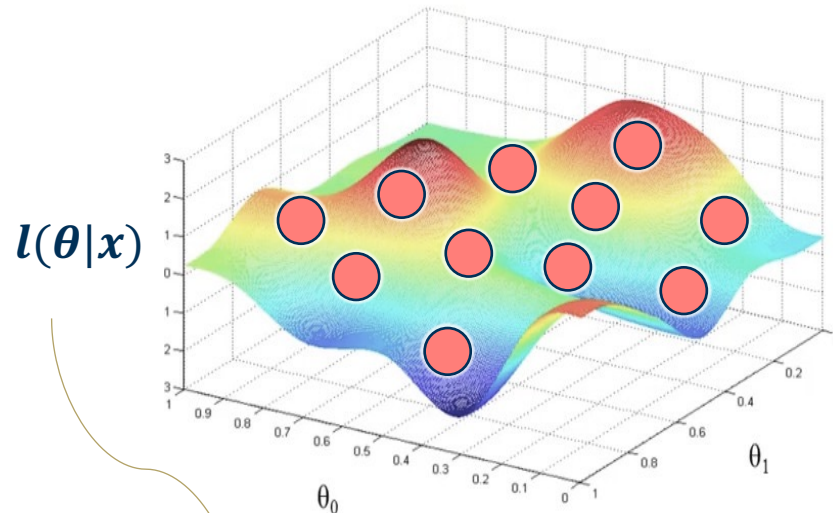
$$I(\theta) = \text{Var}\left(\frac{\partial}{\partial \theta} l(\theta|x)\right)$$

θ = Statistic of distribution
 $l(\theta | x)$ = Likelihood function

Information at Inference

Gradients as Fisher Information

Gradients infer information about the statistics of underlying manifolds



From before, $I(\theta) = \text{Var}\left(\frac{\partial}{\partial \theta} l(\theta|x)\right)$

Using variance decomposition, $I(\theta)$ reduces to:

$I(\theta) = E[U_\theta U_\theta^T]$ where

$E[\cdot]$ = Expectation

$U_\theta = \nabla_\theta l(\theta|x)$, Gradients w.r.t. the sample

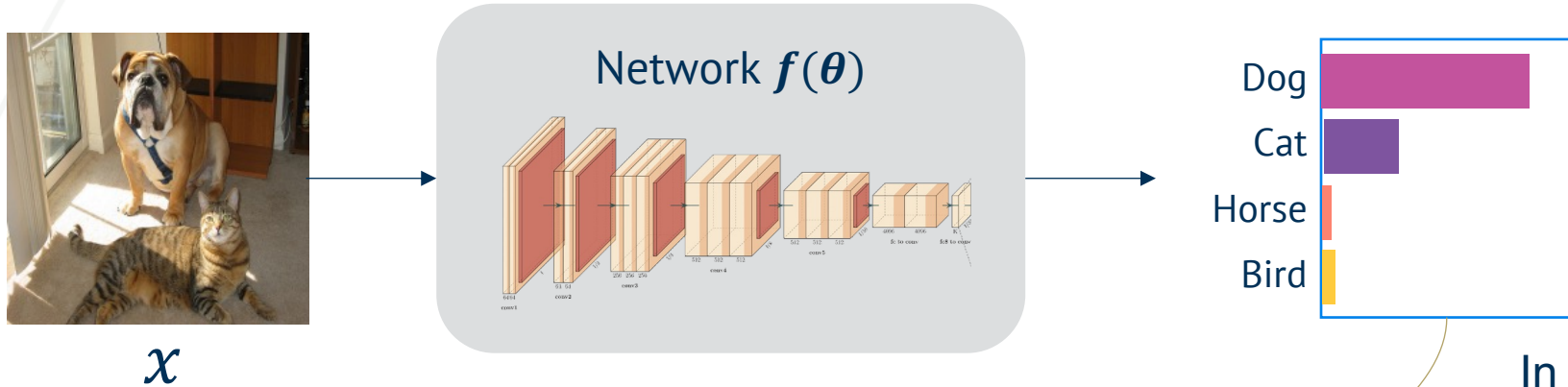
Likelihood function instead of loss manifold

Hence, gradients draw information from the underlying distribution as learned by the network weights!

Information at Inference

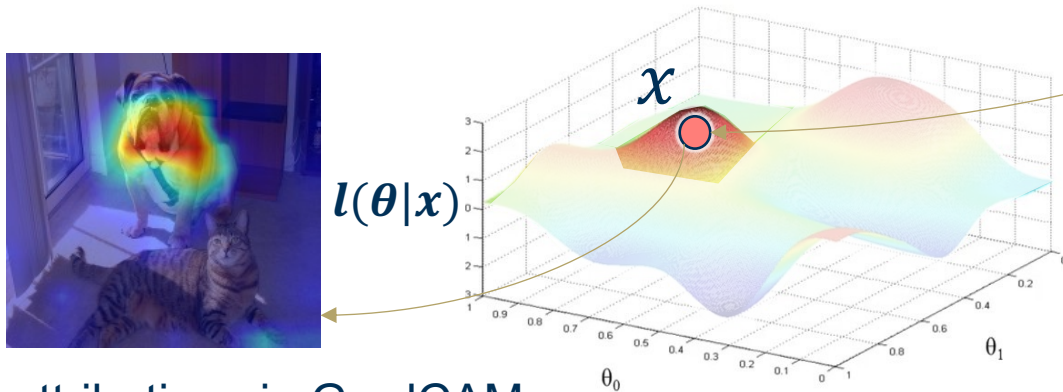
Case Study: Gradients as Fisher Information in Explainability

Gradients infer information about the statistics of underlying manifolds



Local information (specific to x) is sufficient!

In this case, the image and its prediction extracts nose, mouth and jowl features.



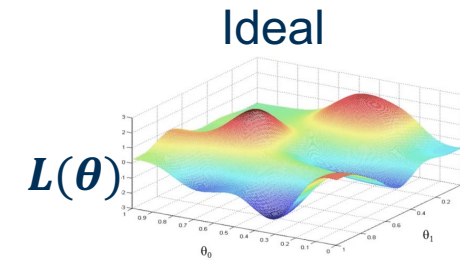
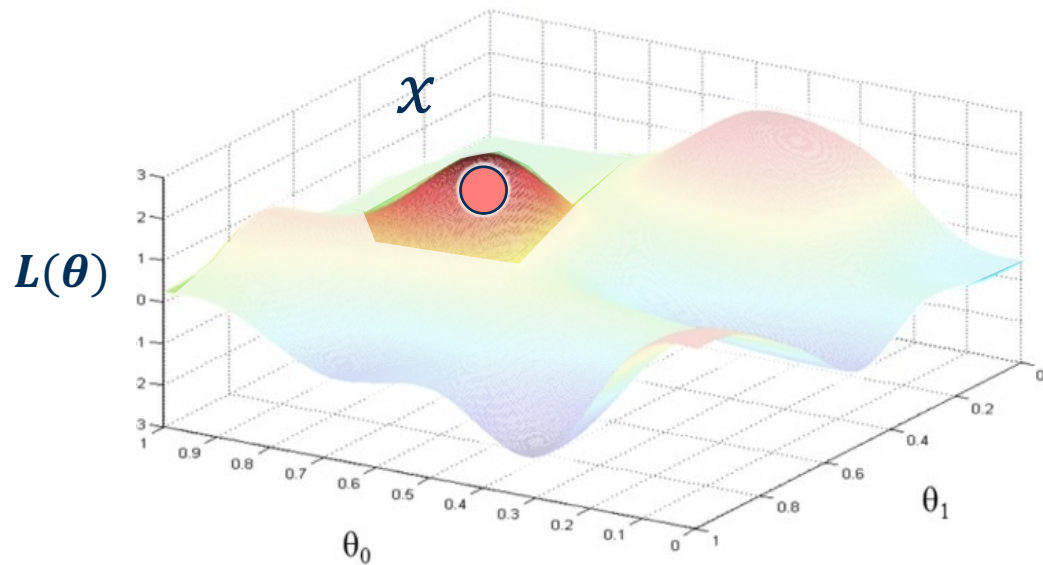
Hence, gradients draw information from the underlying distribution as learned by the network weights!

Feature attribution via GradCAM

Gradients at Inference

Local Information

Gradients provide local information around the vicinity of x , even if x is novel. This is because x projects on the learned knowledge

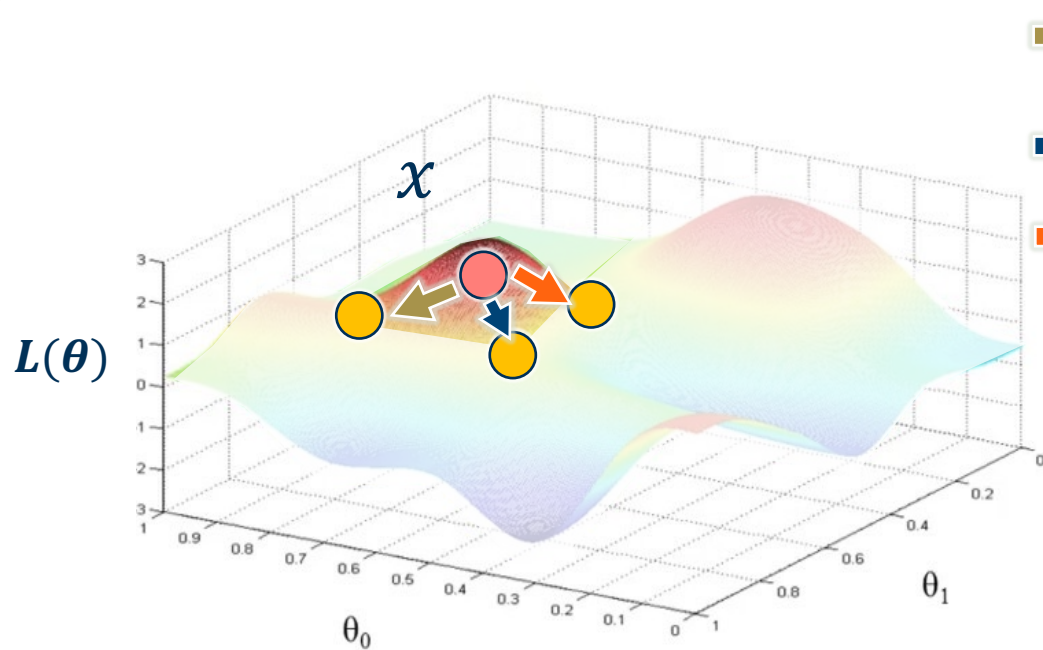


$\alpha \nabla_{\theta} L(\theta)$ provides local information up to a small distance α away from x

Gradients at Inference

Direction of Steepest Descent

Gradients allow choosing the fastest direction of descent given a loss function $L(\theta)$



Path 1?



Path 2?



Path 3?

Which direction should we optimize towards (knowing only the local information)?

Negative of the gradient provides the **descent direction** towards the local minima, as measured by $L(\theta)$

Gradients at Inference

To Characterize the Novel Data at Inference

